

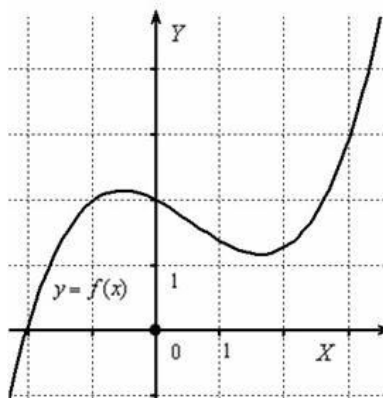
ФГБОУ ВО "Воронежский государственный
технический университет"

Кафедра высшей математики и
физико-математического моделирования

**ИНДИВИДУАЛЬНЫЕ ДОМАШНИЕ ЗАДАНИЯ
К РАЗДЕЛУ
«ВВЕДЕНИЕ В МАТЕМАТИЧЕСКИЙ АНАЛИЗ»**

МЕТОДИЧЕСКИЕ УКАЗАНИЯ

для индивидуальной самостоятельной работы по разделу
«Введение в математический анализ»
курса «Математика» для студентов
направления 11.03.01 «Радиотехника»



Воронеж 2021

**ИНДИВИДУАЛЬНЫЕ ДОМАШНИЕ ЗАДАНИЯ
К РАЗДЕЛУ «НАЧАЛА МАТЕМАТИЧЕСКОГО
АНАЛИЗА»**

Задача 1. Доказать (найти $\delta(\varepsilon)$), что:

$$1.1. \lim_{x \rightarrow 1/2} \frac{2x^2 + 3x - 2}{x - 1/2} = 5.$$

$$1.2. \lim_{x \rightarrow 1/3} \frac{6x^2 - 5x + 1}{x - 1/3} = -1.$$

$$1.3. \lim_{x \rightarrow 3} \frac{x^2 - 4x + 3}{x - 3} = 2.$$

$$1.4. \lim_{x \rightarrow 7/5} \frac{10x^2 + 9x - 7}{x + 7/5} = -19.$$

$$1.5. \lim_{x \rightarrow 1/3} \frac{6x^2 + x - 1}{x - 1/3} = 5.$$

$$1.6. \lim_{x \rightarrow 5/2} \frac{2x^2 - 9x + 10}{2x - 5} = \frac{1}{2}.$$

$$1.7. \lim_{x \rightarrow -1/2} \frac{6x^2 - 75x - 39}{x + 1/2} = -81.$$

$$1.8. \lim_{x \rightarrow 11} \frac{2x^2 - 21x - 11}{x - 11} = 23.$$

$$1.9. \lim_{x \rightarrow 5} \frac{5x^2 - 24x - 5}{x - 5} = 26.$$

$$1.10. \lim_{x \rightarrow 7} \frac{2x^2 + 15x + 7}{x + 7} = -13.$$

$$1.11. \lim_{x \rightarrow -4} \frac{2x^2 + 6x - 8}{x + 4} = -10.$$

$$1.12. \lim_{x \rightarrow -1/3} \frac{6x^2 - x - 1}{3x + 1} = -\frac{5}{3}.$$

$$1.13. \lim_{x \rightarrow -5} \frac{x^2 + 2x - 15}{x + 5} = -8.$$

$$1.14. \lim_{x \rightarrow 8} \frac{3x^2 - 40x + 128}{x - 8} = 8.$$

$$1.15. \lim_{x \rightarrow 10} \frac{5x^2 - 51x + 10}{x - 10} = 49.$$

$$1.16. \lim_{x \rightarrow -6} \frac{3x^2 + 17x - 6}{x + 6} = -19.$$

$$1.17. \lim_{x \rightarrow 1/2} \frac{2x^2 - 5x + 2}{x - 1/2} = -3.$$

$$1.18. \lim_{x \rightarrow 1/3} \frac{3x^2 + 17x - 6}{x - 1/3} = 19.$$

$$1.19. \lim_{x \rightarrow -1/5} \frac{15x^2 - 2x - 1}{x + 1/5} = -8.$$

$$1.20. \lim_{x \rightarrow 1/3} \frac{15x^2 - 2x - 1}{x - 1/3} = 8.$$

$$1.21. \lim_{x \rightarrow 2} \frac{3x^2 - 5x - 2}{x - 2} = 7.$$

$$1.22. \lim_{x \rightarrow -1/3} \frac{3x^2 - 2x - 1}{x + 1/3} = -4.$$

$$1.23. \lim_{x \rightarrow -1/3} \frac{9x^2 - 1}{x + 1/3} = -6.$$

$$1.24. \lim_{x \rightarrow -1} \frac{7x^2 + 8x + 1}{x + 1} = -6.$$

$$1.25. \lim_{x \rightarrow 1/2} \frac{6x^2 - x - 1}{x - 1/2} = 5.$$

$$1.26. \lim_{x \rightarrow -3} \frac{2x^2 + 5x - 3}{x + 3} = -7.$$

$$1.27. \lim_{x \rightarrow -1/2} \frac{6x^2 - x - 1}{x - 1/2} = -5.$$

$$1.28. \lim_{x \rightarrow 3} \frac{4x^2 - 14x + 6}{x - 3} = 10.$$

$$1.29. \lim_{x \rightarrow -2} \frac{3x^2 + 5x - 2}{x + 2} = -7.$$

$$1.30. \lim_{x \rightarrow 1} \frac{5x^2 - 4x - 1}{x - 1} = 6.$$

Задача 2. Найти предел.

$$2.1. \lim_{x \rightarrow 0} (5 + 2x)^{\frac{3}{x+2}}.$$

$$2.2. \lim_{x \rightarrow 1} \frac{x^3 - 3x^2 + 2}{5x^4 + 8x - 6}.$$

$$2.3. \lim_{x \rightarrow 1} \left(\frac{10x - 3}{10x + 1} \right)^{5x}.$$

$$2.4. \lim_{x \rightarrow 4} (4x - 11)^{\frac{5x}{x-3}}.$$

$$2.5. \lim_{x \rightarrow 3} \frac{x^3 - 4x^2 + 6}{2x^3 + 10x^2 + 5x}.$$

$$2.6. \lim_{x \rightarrow \pi/4} \frac{\sin x}{\pi^2 - x^2}.$$

$$2.7. \lim_{x \rightarrow 1} \left(\frac{x^2 + x + 1}{x^2 + 4x - 1} \right)^{-3x^2}.$$

$$2.8. \lim_{x \rightarrow 1} \frac{6x^5 - 3x^2 + 1}{3x^5 - 2x + 3}.$$

$$2.9. \lim_{x \rightarrow \pi/3} \frac{3x^2 - 5x}{\sin 2x}.$$

$$2.10. \lim_{x \rightarrow 1} (2x + 3)^{\frac{4x-2}{x+1}}.$$

$$2.11. \lim_{x \rightarrow 0} \frac{3x^4 - 2}{\sqrt{x^8 + 3x + 4}}.$$

$$2.12. \lim_{x \rightarrow 1} \left(\frac{2x-1}{5x+4} \right)^{x/2}.$$

$$2.13. \lim_{x \rightarrow 3} \frac{(x+1)^3 + (x-1)^3}{x^3 + 1}.$$

$$2.14. \lim_{x \rightarrow \pi/4} \frac{1 - \cos 7x}{3x^2}.$$

$$2.15. \lim_{x \rightarrow 0} (4 - 3x)^{\frac{x}{x-1}}.$$

$$2.16. \lim_{x \rightarrow 1} \frac{(x-3)^2 - (x+3)^2}{(x+2)^2}.$$

$$2.17. \lim_{x \rightarrow 1} \frac{7x^2 - 3x}{2x^2 + 6x - 1}.$$

$$2.18. \lim_{x \rightarrow 1} \left(\frac{x^4}{x^2 + 2} - x^2 \right).$$

$$2.19. \lim_{x \rightarrow 0} (6 - 7x)^{\frac{x+5}{2x-2}}.$$

$$2.20. \lim_{x \rightarrow \pi/4} \frac{\sqrt{1 - \sin x}}{2x - \pi}.$$

$$2.21. \lim_{x \rightarrow 1} \left(\frac{3x^2 - 6x + 7}{3x^2 + 20x - 1} \right)^{1-x}.$$

$$2.22. \lim_{x \rightarrow 1} \frac{x^3 - 4x^2 + 6}{3x^3 + 10x^2 + 4x}.$$

$$2.23. \lim_{x \rightarrow 2} \frac{x^3 - 4x - 2}{5x^3 + 3x^2 - 1}.$$

$$2.24. \lim_{x \rightarrow 1} \left(\frac{13x+2}{13x-15} \right)^{x+7}.$$

$$2.25. \lim_{x \rightarrow 2} \frac{(x+2)^2 - (x-2)^2}{x+2}.$$

$$2.26. \lim_{x \rightarrow 2} \left(\frac{6x-7}{6x+5} \right)^{3x-6}.$$

$$2.27. \lim_{x \rightarrow 0} (2-x)^{\frac{4x+5}{x-1}}.$$

$$2.28. \lim_{x \rightarrow \pi/3} \frac{1 - \cos x}{x^2}.$$

$$2.29. \lim_{x \rightarrow 1} \frac{(3x-4)(x+1)}{x^3 + x^2 + 2}.$$

$$2.30. \lim_{x \rightarrow 0} (2x+3)^{\frac{1}{x+1}}.$$

Задача 3. Найти пределы.

3.1. а) $\lim_{x \rightarrow \infty} \frac{x^5 - 4x^4 + 2}{3x^5 - 2x - 1}$; б) $\lim_{x \rightarrow \infty} \frac{2x^3 + x + 2}{x^2 + 2x + 3}$; в) $\lim_{x \rightarrow \infty} \frac{5x^7 + 2x - 2}{2x^3 - 3x^2 + 1}$.

3.2. а) $\lim_{x \rightarrow \infty} \frac{7x^3 - 4x^2 + 6}{3x^3 + x^2 + x}$; б) $\lim_{x \rightarrow \infty} \frac{x^3 - 3x^2 + 2}{x^4 + 8x - 6}$; в) $\lim_{x \rightarrow \infty} \frac{x^4 - x^2 + 6}{2x^3 + x^2 + x}$.

3.3. а) $\lim_{x \rightarrow \infty} \frac{-4x^3 - 2}{9x^2 + x - 1}$; б) $\lim_{x \rightarrow \infty} \frac{3x^2 - 5x - 1}{3x^3 - 5x^2 + 1}$; в) $\lim_{x \rightarrow \infty} \frac{x^4 - 3x^2 + 2}{5x^4 - 3x - 2}$.

3.4. а) $\lim_{x \rightarrow \infty} \frac{3 - x^2 - 2x}{x^2 + 4x + 1}$; б) $\lim_{x \rightarrow \infty} \frac{x^5 - 5x - 11}{3x^3 - 5x + 1}$; в) $\lim_{x \rightarrow \infty} \frac{x^2 - 4x - 2}{7x^6 - 1}$.

3.5. а) $\lim_{x \rightarrow \infty} \frac{x^3 - x^2 - 2}{x^5 - x + 9}$; б) $\lim_{x \rightarrow \infty} \frac{x^5 - 3x^2 + 1}{3x^5 - 2x + 3}$; в) $\lim_{x \rightarrow \infty} \frac{-3x^4 - 4x - 1}{x^2 + x - 1}$.

3.6. а) $\lim_{x \rightarrow \infty} \frac{3x^5 - 4x - 2}{x^2 + 6x - 5}$; б) $\lim_{x \rightarrow \infty} \frac{x^4 - 4x^2 - 1}{3x^4 + x^2 - 3x}$; в) $\lim_{x \rightarrow \infty} \frac{x^2 - x^3 - 2}{x^4 - x^5 + 4}$.

3.7. а) $\lim_{x \rightarrow \infty} \frac{x^2 - x - 2}{4x^2 + x - 5}$; б) $\lim_{x \rightarrow \infty} \frac{x^4 - x^2 + 6}{2x^3 + x^2 + 4x}$; в) $\lim_{x \rightarrow \infty} \frac{x^3 - 4x^2 - 2}{x^5 + x^2 + x}$.

3.8. а) $\lim_{x \rightarrow \infty} \frac{x^3 - x^2 + 6}{x^6 - x^4 + 3x}$; б) $\lim_{x \rightarrow \infty} \frac{x^5 - 2x + 1}{2x^4 + x^3 - 3}$; в) $\lim_{x \rightarrow \infty} \frac{3x^2 - 4x - 2}{9x^2 + x - 2}$.

3.9. а) $\lim_{x \rightarrow \infty} \frac{2x^4 - 4x^2 - 1}{x^4 + 2x^2 - 3}$; б) $\lim_{x \rightarrow \infty} \frac{x^4 - 3x^5 + 1}{4x^5 - x + 3}$; в) $\lim_{x \rightarrow \infty} \frac{x^5 - 4x^2 + 1}{3x^2 - x + 3}$.

3.10. а) $\lim_{x \rightarrow \infty} \frac{x^2 - 5x - 2}{2x^2 - 5x + 1}$; б) $\lim_{x \rightarrow \infty} \frac{-2x^2 - x}{x^3 + x + 1}$; в) $\lim_{x \rightarrow \infty} \frac{3x^6 - 2x}{x^2 + 2x + 8}$.

$$3.11. \text{ a) } \lim_{x \rightarrow \infty} \frac{x^2 + x - 2}{5x^2 + x - 1}; \text{ б) } \lim_{x \rightarrow \infty} \frac{3x^3 + x - 2}{x^2 + x - 2}; \text{ в) } \lim_{x \rightarrow \infty} \frac{4x - 2}{x^3 + x - 5}.$$

$$3.12. \text{ a) } \lim_{x \rightarrow \infty} \frac{-2x + 3}{x^3 + x + 1}; \text{ б) } \lim_{x \rightarrow \infty} \frac{x^7 - 2x^2 - 4}{x^3 + 9x + 1}; \text{ в) } \lim_{x \rightarrow \infty} \frac{-2x^2 - 3x}{x^2 + 2x + 1}.$$

$$3.13. \text{ a) } \lim_{x \rightarrow \infty} \frac{2x^4 - 5}{x^2 - 4x - 5}; \text{ б) } \lim_{x \rightarrow \infty} \frac{3x^2 + 4x - 2}{6x^2 + x - 5}; \text{ в) } \lim_{x \rightarrow \infty} \frac{-x^2 - 3}{x^3 + 7x + 1}.$$

$$3.14. \text{ a) } \lim_{x \rightarrow \infty} \frac{3x^2 - 2}{-2x^2 + x - 1}; \text{ б) } \lim_{x \rightarrow \infty} \frac{x^3 - 7x + 1}{x^2 + 8x + 5}; \text{ в) } \lim_{x \rightarrow \infty} \frac{x^3 - 4x^2 - 2}{x^5 + x^2 + x}.$$

$$3.15. \text{ a) } \lim_{x \rightarrow \infty} \frac{x^2 - 5x - 2}{9x^2 - 5x + 1}; \text{ б) } \lim_{x \rightarrow \infty} \frac{7x^2 - 1}{x^7 + 7x^2 + x}; \text{ в) } \lim_{x \rightarrow \infty} \frac{x^8 - 1}{x^5 + 2x^2 + 1}.$$

$$3.16. \text{ a) } \lim_{x \rightarrow \infty} \frac{x^4 - x}{x^2 + x - 1}; \text{ б) } \lim_{x \rightarrow \infty} \frac{x^3 + x - 3}{-2x^3 - 3x}; \text{ в) } \lim_{x \rightarrow \infty} \frac{x^2 + 8x + 1}{2x^8 - 3x}.$$

$$3.17. \text{ a) } \lim_{x \rightarrow \infty} \frac{-3x^2 - x + 3}{x^2 + 3x + 1}; \text{ б) } \lim_{x \rightarrow \infty} \frac{x^7 - x + 7}{x^3 + 3x + 1}; \text{ в) } \lim_{x \rightarrow \infty} \frac{x^2 - 3x}{x^5 + 5x + 1}.$$

$$3.18. \text{ a) } \lim_{x \rightarrow \infty} \frac{x^3 - 2x^2 + 6}{2x^3 + x}; \text{ б) } \lim_{x \rightarrow \infty} \frac{x^2 - 1}{x^5 + x^2 + x}; \text{ в) } \lim_{x \rightarrow \infty} \frac{x^4 - x^2 + 2}{2x^2 + x}.$$

$$3.19. \text{ a) } \lim_{x \rightarrow \infty} \frac{4x^3 - 4x^2 - 2}{3x^5 + x^2 + 4x}; \text{ б) } \lim_{x \rightarrow \infty} \frac{-x^2 - 2x}{x^2 + 4x + 1}; \text{ в) } \lim_{x \rightarrow \infty} \frac{x^3 - 2x + 1}{2x^2 + x + 5}.$$

$$3.20. \text{ a) } \lim_{x \rightarrow \infty} \frac{x^2 + 5x + 1}{-2x^2 - 3x}; \text{ б) } \lim_{x \rightarrow \infty} \frac{-x^3 - 2}{2x^2 + x - 3}; \text{ в) } \lim_{x \rightarrow \infty} \frac{x^2 - 3x}{5x^4 + 6x - 1}.$$

$$3.21. \text{ a) } \lim_{x \rightarrow \infty} \frac{2x^2 - 3x + 1}{3x^2 + x + 4}; \text{ б) } \lim_{x \rightarrow \infty} \frac{4x^4 - x^3 - 2}{5x^3 + x^2 - 1}; \text{ в) } \lim_{x \rightarrow \infty} \frac{x^2 - 3x + 4}{x^3 + 5x - 1}.$$

$$3.22. \text{ a) } \lim_{x \rightarrow \infty} \frac{x^2 - 25}{x^2 - 4x - 5}; \text{ б) } \lim_{x \rightarrow \infty} \frac{x^2 - 3x - 4}{x^3 - 5x^2 + 4}; \text{ в) } \lim_{x \rightarrow \infty} \frac{x^7 - 7}{x^2 + 2x - 3}.$$

$$3.23. \text{ a) } \lim_{x \rightarrow \infty} \frac{6x^4 - 3x^5 + 1}{4x^5 - 2x + 3}; \text{ б) } \lim_{x \rightarrow \infty} \frac{x^4 - 4x^2 - 1}{3x^4 + x - 3}; \text{ в) } \lim_{x \rightarrow \infty} \frac{x^6 - x^3 - 2}{x^2 - x^5 + 4}.$$

$$3.24. \text{ a) } \lim_{x \rightarrow \infty} \frac{x^5 - 4x^2 + 1}{3x^5 - 9x + 3}; \text{ б) } \lim_{x \rightarrow \infty} \frac{6x^3 - x^2 + 1}{3x^6 - x + 3}; \text{ в) } \lim_{x \rightarrow \infty} \frac{3x^4 - 2x + 1}{2x^2 + x^3 - 3}.$$

$$3.25. \text{ a) } \lim_{x \rightarrow \infty} \frac{4x^4 - 4x^3}{5x^2 + 3x^2 - 1}; \text{ б) } \lim_{x \rightarrow \infty} \frac{-3x^5 - 2}{x^5 + x^4 - x}; \text{ в) } \lim_{x \rightarrow \infty} \frac{x^2 - x - 2}{2x^3 - x^4 + 1}.$$

$$3.26. \text{ a) } \lim_{x \rightarrow \infty} \frac{x^3 - 4x^2 + 6}{4x^3 - x^4 + 4x}; \text{ б) } \lim_{x \rightarrow \infty} \frac{x^3 - 2x + 1}{2x^4 + x + 5}; \text{ в) } \lim_{x \rightarrow \infty} \frac{x^4 - 3x + 4}{2x^3 + 5x - 1}.$$

$$3.27. \text{ a) } \lim_{x \rightarrow \infty} \frac{3x^2 + 4x - 2}{-6x^4 - 5}; \text{ б) } \lim_{x \rightarrow \infty} \frac{x^3 - 4x^2 + 6}{2x^3 - x^2 + x}; \text{ в) } \lim_{x \rightarrow \infty} \frac{2x^5 - 5}{3x^3 - 5x}.$$

$$3.28. \text{ a) } \lim_{x \rightarrow \infty} \frac{3x^2 - 5x - 1}{3x^3 - x^2 + 1}; \text{ б) } \lim_{x \rightarrow \infty} \frac{x^3 - 4x - 2}{5x^3 + x^2 - 1}; \text{ в) } \lim_{x \rightarrow \infty} \frac{x^2 - 4x - 2}{x + 7x^2 - 1}.$$

$$3.29. \text{ a) } \lim_{x \rightarrow \infty} \frac{6x^2 + 3x}{2x^2 - 3x + 5}; \text{ б) } \lim_{x \rightarrow \infty} \frac{5x^3 - x + 1}{2x^2 - 3}; \text{ в) } \lim_{x \rightarrow \infty} \frac{7x^2 - 3x}{2x^7 + 6x - 1}.$$

$$3.30. \text{ a) } \lim_{x \rightarrow \infty} \frac{3x^8 - 4x - 2}{9x^2 + 2x}; \text{ б) } \lim_{x \rightarrow \infty} \frac{2x^2 + x - 8}{3x^4 - 5x}; \text{ в) } \lim_{x \rightarrow \infty} \frac{x^3 - 4x^2 + 6}{2x^3 + x^2 + x}.$$

Задача 4. Найти предел.

$$4.1. \lim_{x \rightarrow \infty} \frac{x^3 \sqrt{5x^2} + \sqrt[4]{9x^8 + 1}}{(x + \sqrt{x}) \sqrt{7-x+x^2}}.$$

$$4.2. \lim_{x \rightarrow \infty} \frac{\sqrt{x^3 + 1} - \sqrt{x-1}}{\sqrt[3]{x^3 + 1} - \sqrt{x-1}}.$$

$$4.3. \lim_{x \rightarrow \infty} \frac{\sqrt{x-1} + \sqrt{x^2 + 1}}{\sqrt[3]{3x^3 + 3} + \sqrt[4]{x^5 + 1}}.$$

$$4.4. \lim_{x \rightarrow \infty} \frac{\sqrt[3]{x^2 - 1} + 7x^3}{\sqrt[4]{x^{12} + x + 1} - x}.$$

$$4.5. \lim_{x \rightarrow \infty} \frac{\sqrt{3x-1} + \sqrt[3]{125x^3 + x}}{\sqrt[3]{x} - x}.$$

$$4.6. \lim_{x \rightarrow \infty} \frac{\sqrt{x^6 + 4} + \sqrt{x-4}}{\sqrt[5]{x^6 + 6} - \sqrt{x-6}}.$$

$$4.7. \lim_{x \rightarrow \infty} \frac{x^5 \sqrt{x} + \sqrt[3]{125x^3 + x}}{(x + \sqrt[4]{x}) \sqrt{9+x^2}}.$$

$$4.8. \lim_{x \rightarrow \infty} \frac{4x^2 - \sqrt[4]{x^3}}{\sqrt[3]{x^6 + x^3 + 1} - 5x}.$$

$$4.9. \lim_{x \rightarrow \infty} \frac{\sqrt{x+2} - \sqrt{x^2 + 2}}{\sqrt[4]{4x^4 + 1} - \sqrt[3]{x^4 - 1}}.$$

$$4.10. \lim_{x \rightarrow \infty} \frac{\sqrt{x+3} - \sqrt[3]{8x^3 + 3}}{\sqrt[4]{x+4} - \sqrt[5]{x^5 + 5}}.$$

$$4.11. \lim_{x \rightarrow \infty} \frac{\sqrt{x^4 + 2} + \sqrt{x-2}}{\sqrt[4]{x^4 + 2} + \sqrt{x-2}}.$$

$$4.12. \lim_{x \rightarrow \infty} \frac{x^4 \sqrt{11x} + \sqrt{25x^4 - 81}}{(x - 7\sqrt{x}) \sqrt{x^2 - x + 1}}.$$

$$4.13. \lim_{x \rightarrow \infty} \frac{6x^3 - \sqrt{x^5 + 1}}{\sqrt{4x^6 + 3} - x}.$$

$$4.14. \lim_{x \rightarrow \infty} \frac{\sqrt[3]{x^2} - \sqrt{x^2 + 5}}{\sqrt[5]{x^7} - \sqrt{x+1}}.$$

$$4.15. \lim_{x \rightarrow \infty} \frac{\sqrt{5x+2} - \sqrt[5]{8x^3 + 5}}{\sqrt[4]{x+7} - x}.$$

$$4.16. \lim_{x \rightarrow \infty} \frac{\sqrt{x^7 + 5} - \sqrt{x-5}}{\sqrt[7]{x^7 + 5} + \sqrt{x-5}}.$$

$$4.17. \lim_{n \rightarrow \infty} \frac{x^4 \sqrt{3x+1} + \sqrt{81x^4 + 1}}{(x + \sqrt[3]{x}) \sqrt{5-x+x^2}}.$$

$$4.18. \lim_{n \rightarrow \infty} \frac{\sqrt[3]{x^2 + 2} - 5x^2}{x - \sqrt{x^4 - x + 1}}.$$

$$4.19. \lim_{x \rightarrow \infty} \frac{\sqrt{x+3} - \sqrt{x^2-3}}{\sqrt[3]{x^5-4} - \sqrt{x^4+1}}.$$

$$4.20. \lim_{x \rightarrow \infty} \frac{\sqrt{x+2} - \sqrt[3]{x^3+2}}{\sqrt[7]{x+2} - \sqrt[5]{x^5+2}}.$$

$$4.21. \lim_{x \rightarrow \infty} \frac{\sqrt[3]{x} - 9x^2}{3x - \sqrt[4]{9x^8+1}}.$$

$$4.22. \lim_{x \rightarrow \infty} \frac{x\sqrt{71x} - \sqrt[3]{64x^6+9}}{(x - \sqrt[3]{x})\sqrt{11+x^2}}.$$

$$4.23. \lim_{x \rightarrow \infty} \frac{\sqrt{4x+1} - \sqrt[3]{27x^3+4}}{4\sqrt{x} - \sqrt[3]{x^5+x}}.$$

$$4.24. \lim_{x \rightarrow \infty} \frac{\sqrt{x+6} - \sqrt{x^2-5}}{\sqrt[3]{x^3+3} + \sqrt[4]{x^3+1}}.$$

$$4.25. \lim_{x \rightarrow \infty} \frac{\sqrt{x^8+6} - \sqrt{x-6}}{\sqrt[8]{x^8+6} + \sqrt{x-6}}.$$

$$4.26. \lim_{x \rightarrow \infty} \frac{x\sqrt[3]{7x} - \sqrt[4]{81x^8-1}}{(x+4\sqrt{x})\sqrt{x^2-5}}.$$

$$4.27. \lim_{x \rightarrow \infty} \frac{\sqrt[3]{x^3-7} + \sqrt[3]{x^2+4}}{\sqrt[4]{x^5+5} + \sqrt{x}}.$$

$$4.28. \lim_{x \rightarrow \infty} \frac{x^2 - \sqrt{x^3+1}}{\sqrt[3]{x^6+2} - x}.$$

$$4.29. \lim_{x \rightarrow \infty} \frac{x^4\sqrt{13x} + \sqrt{x^4-81}}{(x-7\sqrt{x})\sqrt{x^2-x+1}}.$$

$$4.30. \lim_{x \rightarrow \infty} \frac{\sqrt{2x+1} - \sqrt{x^2+2}}{\sqrt[4]{6x^4+1} - \sqrt[3]{3x^4-1}}.$$

Задача 5. Найти предел.

$$5.1. \lim_{x \rightarrow \infty} (\sqrt{x+4} - x).$$

$$5.2. \lim_{x \rightarrow \infty} (\sqrt{x^2+1} - \sqrt{x^2-1}).$$

$$5.3. \lim_{x \rightarrow \infty} x(\sqrt{x(x-2)} - \sqrt{x^2-3}).$$

$$5.4. \lim_{x \rightarrow \infty} x(\sqrt{x+1} - x).$$

$$5.5. \lim_{x \rightarrow \infty} (\sqrt{x^2+2} - \sqrt{x^2+3}).$$

$$5.6. \lim_{x \rightarrow \infty} (\sqrt{(x+1)(x-2)} - x).$$

$$5.7. \lim_{x \rightarrow \infty} (\sqrt{x+7} - \sqrt{x}).$$

$$5.8. \lim_{x \rightarrow \infty} (x - \sqrt{x^2+x+1}).$$

$$5.9. \lim_{x \rightarrow \infty} (\sqrt{x(x+6)} - x).$$

$$5.10. \lim_{x \rightarrow \infty} (\sqrt{x^2+4} - \sqrt{x^2-2}).$$

5.11. $\lim_{x \rightarrow \infty} \sqrt{x}(\sqrt{x+2} - \sqrt{x-3})$.

5.12. $\lim_{x \rightarrow \infty} x(\sqrt{x^4+3} - \sqrt{x^4-2})$.

5.13. $\lim_{x \rightarrow \infty} (\sqrt{x(x+3)} - x)$.

5.14. $\lim_{x \rightarrow \infty} (\sqrt{x^2+3x} - \sqrt{x^2-1})$.

5.15. $\lim_{x \rightarrow \infty} (\sqrt{x^2+2x+1} - x)$.

5.16. $\lim_{x \rightarrow \infty} (\sqrt{x^2+2} - \sqrt{x^2+1})$.

5.17. $\lim_{x \rightarrow \infty} (\sqrt{x^2-3x+2} - x)$.

5.18. $\lim_{x \rightarrow \infty} (\sqrt{x^2+1} - x)$.

5.19. $\lim_{x \rightarrow \infty} (\sqrt{x-3} - \sqrt{x})$.

5.20. $\lim_{x \rightarrow \infty} x(\sqrt{x^2+1} - \sqrt{x})$.

5.21. $\lim_{x \rightarrow \infty} x(\sqrt{x^2+3} - \sqrt{x^2-3})$.

5.22. $\lim_{x \rightarrow \infty} x(\sqrt{x+3} - x)$.

5.23. $\lim_{x \rightarrow \infty} x(\sqrt{x-2} - \sqrt{x-3})$.

5.24. $\lim_{x \rightarrow \infty} x(\sqrt{x-5} - x)$.

5.25. $\lim_{x \rightarrow \infty} (\sqrt{x+3} - \sqrt{x})$.

5.26. $\lim_{x \rightarrow \infty} (\sqrt{x(x+2)} - x)$.

5.27. $\lim_{x \rightarrow \infty} x(\sqrt{x^2+2} - \sqrt{x^2-2})$.

5.28. $\lim_{x \rightarrow \infty} (\sqrt{(x+2)(x-3)} - x)$.

5.29. $\lim_{x \rightarrow \infty} x(x - \sqrt{x+1})$.

5.30. $\lim_{x \rightarrow \infty} (\sqrt{x^2-5x+6} - x)$.

Задача 6. Найти предел.

6.1. $\lim_{x \rightarrow -4} \frac{x^2+14x+40}{8x^2+25x-28}$.

6.2. $\lim_{x \rightarrow 5} \frac{2x^2-9x-5}{x^2-6x+5}$.

4.3. $\lim_{x \rightarrow -2} \frac{6x^2+7x-10}{x^2-4}$.

6.4. $\lim_{x \rightarrow 4} \frac{3x^2-10x-8}{2x^2-9x+4}$.

6.5. $\lim_{x \rightarrow 5} \frac{3x^2-14x-5}{2x^2-13x+15}$.

6.6. $\lim_{x \rightarrow -3} \frac{4x^2+11x-3}{3x^2+14x+15}$.

$$6.7. \lim_{x \rightarrow 3} \frac{3x^2 - 8x - 3}{2x^2 - 11x + 15}.$$

$$6.8. \lim_{x \rightarrow 6} \frac{x^2 - x - 30}{2x^2 - 11x - 6}.$$

$$6.9. \lim_{x \rightarrow 7} \frac{x^2 + x - 56}{x^2 - 49}.$$

$$6.10. \lim_{x \rightarrow 1} \frac{x^3 - 1}{x^2 - 2x + 1}.$$

$$6.11. \lim_{x \rightarrow 3} \frac{2x^2 - 7x + 3}{x - 3}.$$

$$6.12. \lim_{x \rightarrow -2} \frac{x^2 + 3x + 2}{2x^2 + 10x + 12}.$$

$$6.13. \lim_{x \rightarrow 3} \frac{x^3 - 27}{x^2 - 9}.$$

$$6.14. \lim_{x \rightarrow 1} \frac{2x^2 - 3x + 1}{x^2 - 1}.$$

$$6.15. \lim_{x \rightarrow 2} \frac{x^2 - 5x + 6}{x^2 - x - 2}.$$

$$6.16. \lim_{x \rightarrow 5} \frac{x^2 + 3x - 10}{x^2 - 25}.$$

$$6.17. \lim_{x \rightarrow -1} \frac{2x^2 + x - 1}{x^2 - 6x - 7}.$$

$$6.18. \lim_{x \rightarrow 4} \frac{x^2 + x - 12}{x^2 + 2x - 8}.$$

$$6.19. \lim_{x \rightarrow 3} \frac{5x^2 - 2x - 39}{-x^2 - 2x + 15}.$$

$$6.20. \lim_{x \rightarrow 3} \frac{x^2 + x - 12}{3x - 9}.$$

$$6.21. \lim_{x \rightarrow 0,5} \frac{4x^2 - 8x + 3}{2x^2 - 7x + 3}.$$

$$6.22. \lim_{x \rightarrow 5} \frac{3x^2 - 14x - 5}{x^2 - 6x + 5}.$$

$$6.23. \lim_{x \rightarrow 2} \frac{x^3 - 8}{2x - 4}.$$

$$6.24. \lim_{x \rightarrow -2} \frac{3x^2 + 5x - 2}{2x^2 + 3x - 2}.$$

$$6.25. \lim_{x \rightarrow 3} \frac{2x^2 - 7x + 3}{5x^2 - 16x + 3}.$$

$$6.26. \lim_{x \rightarrow 3} \frac{2x^2 - 5x - 3}{x^2 - 5x + 6}.$$

$$6.27. \lim_{x \rightarrow 2} \frac{x^2 - 3x + 2}{x - 2}.$$

$$6.28. \lim_{x \rightarrow 3} \frac{x^2 - 5x + 6}{x^2 - 2x - 3}.$$

$$6.29. \lim_{x \rightarrow -7} \frac{x^2 + 4x - 21}{x + 7}.$$

$$6.30. \lim_{x \rightarrow 1} \frac{2x^2 - x - 1}{3x^2 + x - 4}.$$

Задача 7. Найти предел.

$$7.1. \lim_{x \rightarrow 1} \frac{\sqrt{5x+4}-3}{\sqrt{2x-1}-1}.$$

$$7.2. \lim_{x \rightarrow 2} \frac{x-2}{\sqrt{4x+1}-3}.$$

$$7.3. \lim_{x \rightarrow 4} \frac{\sqrt{1+2x}-3}{\sqrt{x}-2}.$$

$$7.4. \lim_{x \rightarrow -8} \frac{\sqrt{1-x}-3}{2+\sqrt[3]{x}}.$$

$$7.5. \lim_{x \rightarrow -2} \frac{\sqrt[3]{x-4}+2}{x^3+27}.$$

$$7.6. \lim_{x \rightarrow 5} \frac{\sqrt{x-1}-2}{\sqrt{2x-1}-3}.$$

$$7.7. \lim_{x \rightarrow -2} \frac{\sqrt[3]{x-6}+2}{x^3+8}.$$

$$7.8. \lim_{x \rightarrow 0} \frac{\sqrt{x+9}-3}{x^2+x}.$$

$$7.9. \lim_{x \rightarrow -1} \frac{\sqrt{2x+3}-1}{\sqrt{5+x}-2}.$$

$$7.10. \lim_{x \rightarrow 0} \frac{1-\sqrt{2x+1}}{x}.$$

$$7.11. \lim_{x \rightarrow -1} \frac{\sqrt{2x+3}-1}{\sqrt{5+x}-2}.$$

$$7.12. \lim_{x \rightarrow -1} \frac{\sqrt{x^2+3}+2x}{x+1}.$$

$$7.13. \lim_{x \rightarrow 0} \frac{\sqrt{1+x+x^2}-1}{x}.$$

$$7.14. \lim_{x \rightarrow 3} \frac{x-3}{\sqrt[3]{x^2-1}-2}.$$

$$7.15. \lim_{x \rightarrow 2} \frac{x-2}{\sqrt{4x+1}-3}.$$

$$7.16. \lim_{x \rightarrow 6} \frac{\sqrt{x-5}-1}{36-x^2}.$$

$$7.17. \lim_{x \rightarrow 7} \frac{\sqrt{x-3}-2}{x^2-49}.$$

$$7.18. \lim_{x \rightarrow -8} \frac{\sqrt{1-x}-3}{2+\sqrt[3]{x}}.$$

$$7.19. \lim_{x \rightarrow 0} \frac{1-\sqrt{1-x}}{1-\sqrt[3]{1+x}}.$$

$$7.20. \lim_{x \rightarrow -3} \frac{\sqrt{x+4}-1}{x+3}.$$

7.21. $\lim_{x \rightarrow 0} \frac{\sqrt{x+4} - 2}{x}$.

7.22. $\lim_{x \rightarrow 1} \frac{\sqrt{x+3} - 2}{1 - \sqrt{2-x}}$.

7.23. $\lim_{x \rightarrow 0} \frac{\sqrt{x+9} - 3}{\sqrt{1-x} - 1}$.

7.24. $\lim_{x \rightarrow -1} \frac{x+1}{\sqrt{x+5} - 2}$.

7.25. $\lim_{x \rightarrow 2} \frac{\sqrt{x+2} - 2}{\sqrt{x-1} - 1}$.

7.26. $\lim_{x \rightarrow 0} \frac{1 - \sqrt{1-x}}{2 - \sqrt[3]{8-x}}$.

7.27. $\lim_{x \rightarrow 2} \frac{\sqrt{x^2-1} - \sqrt{x+x^2-3}}{x^2-4}$.

7.28. $\lim_{x \rightarrow 1} \frac{\sqrt{x}-1}{1-\sqrt{1-x}}$.

7.29. $\lim_{x \rightarrow -2} \frac{\sqrt{x+11} - 3}{x^2 + 2x}$.

7.30. $\lim_{x \rightarrow 0} \frac{\sqrt{1+x} - \sqrt{1-x}}{3x}$.

Задача 8. Найти предел.

8.1. $\lim_{x \rightarrow 0} \frac{\sin 5x^2}{3x^2}$.

8.2. $\lim_{x \rightarrow 0} \frac{\sin \sqrt{3x}}{\sin 6x}$.

8.3. $\lim_{x \rightarrow 0} \frac{\sin^2(x/2)}{x^2}$.

8.4. $\lim_{x \rightarrow 0} \frac{\operatorname{tg} 2x^2}{4x^2}$.

8.5. $\lim_{x \rightarrow 0} \frac{\operatorname{arctg}(x/2)}{x}$.

8.6. $\lim_{x \rightarrow 0} \frac{\sin 2x^2}{4x^2}$.

8.7. $\lim_{x \rightarrow 0} \frac{4x^2}{\sin 9x^2}$.

8.8. $\lim_{x \rightarrow 0} \frac{\operatorname{arctg}(x/2)}{\arcsin(x/7)}$.

8.9. $\lim_{x \rightarrow 0} \frac{\operatorname{tg}^2 x}{\sin^2 3x}$.

8.10. $\lim_{x \rightarrow 0} \frac{\arcsin 3x}{\sin 2x}$.

8.11. $\lim_{x \rightarrow 0} \frac{\operatorname{tg}^2(x/3)}{\sin^2(x/4)}.$

8.12. $\lim_{x \rightarrow 0} \frac{x^2}{\operatorname{arctg}^2 4x}.$

8.13. $\lim_{x \rightarrow 0} \frac{\operatorname{arctg}^3(x/2)}{\operatorname{arcsin}^2(x/3)}.$

8.14. $\lim_{x \rightarrow 0} \frac{x^2}{\sin^2(2x/3)}.$

8.15. $\lim_{x \rightarrow 0} \frac{\operatorname{arcsin}(x^3/8)}{\sin^3(x/2)}.$

8.16. $\lim_{x \rightarrow 0} \frac{\sin \sqrt{3x}}{\operatorname{arcsin} \sqrt{x}}.$

8.17. $\lim_{x \rightarrow 0} \frac{\sin(3x/2)}{\sin x^2}.$

8.18. $\lim_{x \rightarrow 0} \frac{\operatorname{tg}(x/2)}{\sin(x/5)}.$

8.19. $\lim_{x \rightarrow 0} \frac{\operatorname{tg}^2(x/2)}{\operatorname{arcsin}^2(x/3)}.$

8.20. $\lim_{x \rightarrow 0} \frac{\operatorname{tg}^3(x/5)}{\sin^3(x/2)}.$

8.21. $\lim_{x \rightarrow 0} \frac{\operatorname{arctg}^2 5x}{x^2}.$

8.22. $\lim_{x \rightarrow 0} \frac{\sin 2x^2}{\operatorname{arcsin}^2 4x}.$

8.23. $\lim_{x \rightarrow 0} \frac{x^4}{\sin^3(x/2)}.$

8.24. $\lim_{x \rightarrow 0} \frac{x^2}{\sin 5x^2}.$

8.25. $\lim_{x \rightarrow 0} \frac{\sin 5x^3}{3x^3}.$

8.26. $\lim_{x \rightarrow 0} \frac{x^2}{\operatorname{tg}^2(x/7)}.$

8.27. $\lim_{x \rightarrow 0} \frac{\sin 2x^2}{4x^2}.$

8.28. $\lim_{x \rightarrow 0} \frac{x^2}{\sin^2(x/2)}.$

8.29. $\lim_{x \rightarrow 0} \frac{\sin^2 x}{\sin^2 5x}.$

8.30. $\lim_{x \rightarrow 0} \frac{\operatorname{arc} \sin 5x^2}{x^2}.$

Задача 9. Найти предел.

$$9.1. \lim_{x \rightarrow 0} \frac{1 - \cos 4x}{1 - \cos 8x}.$$

$$9.2. \lim_{x \rightarrow 0} \frac{\sin 5x - \sin 3x}{\sin x}.$$

$$9.3. \lim_{x \rightarrow 0} \frac{1 - \cos 3x}{4x^2}.$$

$$9.4. \lim_{x \rightarrow 0} \frac{1 - \cos 5x}{x \operatorname{tg} 2x}.$$

$$9.5. \lim_{x \rightarrow 0} \frac{\operatorname{tg} x - \sin x}{x^3}.$$

$$9.6. \lim_{x \rightarrow 0} \frac{1 - \cos 2x}{x \sin x}.$$

$$9.7. \lim_{x \rightarrow 0} \frac{\sin x - \operatorname{tg} x}{\sin^3 x}.$$

$$9.6. \lim_{x \rightarrow 0} \frac{\cos 4x - 1}{\operatorname{tg}^2 2x}.$$

$$9.9. \lim_{x \rightarrow 0} \frac{\cos 4x - \cos 6x}{\sin^2 5x}.$$

$$9.10. \lim_{x \rightarrow 0} \frac{\sin x - \sin 2x}{x^2}.$$

$$9.11. \lim_{x \rightarrow 0} (1 - \cos 5x) \cdot \operatorname{ctg}^2 3x.$$

$$9.12. \lim_{x \rightarrow 0} \frac{1 - \cos 7x}{3x^2}.$$

$$9.13. \lim_{x \rightarrow 0} \frac{\cos x - \cos 3x}{x^2}.$$

$$9.14. \lim_{x \rightarrow 0} \frac{\cos x - \cos^3 x}{x \sin 2x}.$$

$$9.15. \lim_{x \rightarrow 0} \frac{\sin^2 x - \operatorname{tg}^2 x}{x^4}.$$

$$9.16. \lim_{x \rightarrow 0} \frac{2x \cdot \sin x}{1 - \cos x}.$$

$$9.17. \lim_{x \rightarrow 0} \frac{\cos 3x - \cos 5x}{\sin^2 3x}.$$

$$9.18. \lim_{x \rightarrow 0} \frac{x^3}{\operatorname{arctg} x + x^3}.$$

$$9.19. \lim_{x \rightarrow 0} \frac{\sin 4x - \sin 6x}{x^2}.$$

$$9.20. \lim_{x \rightarrow 0} \frac{x^2}{\sin 2x - \sin x}.$$

$$9.21. \lim_{x \rightarrow 0} \frac{1 - \cos 2x}{\operatorname{tg}^2 3x}.$$

$$9.22. \lim_{x \rightarrow 0} \frac{1 - \cos 2x}{1 - \cos 6x}.$$

$$9.23. \lim_{x \rightarrow 0} \frac{\cos 2x - \cos 5x}{5x^2}.$$

$$9.24. \lim_{x \rightarrow 0} \frac{\sin^2 3x}{\cos 8x - \cos 2x}.$$

$$9.25. \lim_{x \rightarrow 0} \frac{4x^2}{1 - \cos 3x}.$$

$$9.26. \lim_{x \rightarrow 0} \frac{\cos 2x - \cos 5x}{3x^2}.$$

$$9.27. \lim_{x \rightarrow 0} \frac{x \sin 2x}{1 - \cos 4x}.$$

$$9.28. \lim_{x \rightarrow 0} (1 - \cos x) \cdot \operatorname{ctg}^2 2x.$$

$$9.29. \lim_{x \rightarrow 0} \frac{\cos x - \cos 3x}{\sin^2 4x}.$$

$$9.30. \lim_{x \rightarrow 0} \frac{\operatorname{tg}^2 4x}{1 - \cos 3x}.$$

Задача 10. Найти предел.

$$10.1. \lim_{x \rightarrow -\pi} \frac{\sin 2x}{x(\pi + x)}.$$

$$10.2. \lim_{x \rightarrow \pi/2} \left(\frac{\pi}{2} - x \right) \operatorname{tg} x.$$

$$10.3. \lim_{x \rightarrow \pi/6} \frac{\sin(x - \pi/6)}{\sqrt{3}/2 - \cos x}.$$

$$10.4. \lim_{x \rightarrow 1} \frac{\cos(\pi x/2)}{1 - \sqrt{x}}.$$

$$10.5. \lim_{x \rightarrow \pi/2} \frac{\operatorname{tg} 3x}{\operatorname{tg} x}.$$

$$10.6. \lim_{x \rightarrow \pi} \frac{\sin x}{\pi^2 - x^2}.$$

$$10.7. \lim_{x \rightarrow \pi/4} \operatorname{tg} \left(\frac{\pi}{4} - x \right) \operatorname{tg} 2x.$$

$$10.8. \lim_{x \rightarrow \pi} \frac{\cos(x/2)}{x - \pi}.$$

$$10.9. \lim_{x \rightarrow \pi/2} \frac{\cos x}{\pi - 2x}.$$

$$10.10. \lim_{x \rightarrow \pi/2} \frac{\sqrt{1 - \sin x}}{2x - \pi}.$$

$$10.11. \lim_{x \rightarrow 1} (1 - x) \operatorname{tg} \frac{\pi x}{2}.$$

$$10.12. \lim_{x \rightarrow 2} (x - 2) \operatorname{ctg} \frac{\pi x}{2}.$$

$$10.13. \lim_{x \rightarrow -2} \frac{\operatorname{arctg}(x + 2)}{x^2 - 4}.$$

$$10.14. \lim_{x \rightarrow 1} \frac{\sin \pi x}{\sin 3\pi x}.$$

$$10.15. \lim_{x \rightarrow 1/3} \frac{\sin(1-3x)}{9x^2-1}.$$

$$10.16. \lim_{x \rightarrow 0} (\cos 7x - 1) \cdot \operatorname{ctg} x^2.$$

$$10.17. \lim_{x \rightarrow 4} \frac{\operatorname{tg}(x-4)}{x^2-16}.$$

$$10.18. \lim_{x \rightarrow -5} \frac{\sin(x+5)}{x^2-25}.$$

$$10.19. \lim_{x \rightarrow \pi} \frac{1 - \sin(x/2)}{\pi - x}.$$

$$10.20. \lim_{x \rightarrow -2} \frac{\sin \pi x}{x+2}.$$

$$10.21. \lim_{x \rightarrow 1/2} \frac{\arcsin(1-2x)}{4x^2-1}.$$

$$10.22. \lim_{x \rightarrow \pi/2} \frac{1 - \sin x}{(x - \pi/2)\cos x}.$$

$$10.23. \lim_{x \rightarrow 0} (\cos 3x - 1) \cdot \operatorname{ctg} 2x^2.$$

$$10.24. \lim_{x \rightarrow \pi/3} (3x - \pi) \sin \frac{x}{3x - \pi}.$$

$$10.25. \lim_{x \rightarrow \pi} \frac{\sin 3x}{\sin x}.$$

$$10.26. \lim_{x \rightarrow \pi/3} \left(\frac{\pi}{3} - x \right) \operatorname{tg}(3x/2).$$

$$10.27. \lim_{x \rightarrow \pi/3} \operatorname{tg} \left(\frac{\pi}{3} - x \right) \operatorname{tg} 3x.$$

$$10.28. \lim_{x \rightarrow -3} \frac{\operatorname{tg}(x+3)}{x^2-9}.$$

$$10.29. \lim_{x \rightarrow \pi/2} (2x - \pi) \sin \frac{x}{2x - \pi}.$$

$$10.30. \lim_{x \rightarrow -1/2} \frac{\operatorname{arctg}(2x+1)}{4x^2-1}.$$

Задача 11. Найти предел.

$$11.1. \lim_{x \rightarrow \infty} \left(\frac{x+1}{x-1} \right)^x.$$

$$11.2. \lim_{x \rightarrow \infty} \left(\frac{x^2+x+1}{x^2+x-1} \right)^{-x^2}.$$

$$11.3. \lim_{x \rightarrow \infty} \left(\frac{2x+3}{2x+1} \right)^{x+1}.$$

$$11.4. \lim_{x \rightarrow \infty} \left(\frac{x-1}{x+1} \right)^{x^2}.$$

$$11.5. \lim_{x \rightarrow \infty} \left(\frac{2x^2 + 5x + 7}{2x^2 + 5x + 3} \right)^x.$$

$$11.6. \lim_{x \rightarrow \infty} \left(\frac{x-1}{x+3} \right)^{x+2}.$$

$$11.7. \lim_{x \rightarrow \infty} \left(\frac{x^2 - 1}{x^2} \right)^{x^4}.$$

$$11.8. \lim_{x \rightarrow \infty} \left(\frac{5x^2 + 3x - 1}{5x^2 + 3x + 3} \right)^x.$$

$$11.9. \lim_{x \rightarrow \infty} \left(\frac{2x^2 + 2}{2x^2 + 1} \right)^{x^2}.$$

$$11.10. \lim_{x \rightarrow \infty} \left(\frac{2x^2 + 7x - 1}{2x^2 + 3x - 1} \right)^{-x^3}.$$

$$11.11. \lim_{x \rightarrow \infty} \left(\frac{3x+1}{3x-1} \right)^{2x+3}.$$

$$11.12. \lim_{x \rightarrow \infty} \left(\frac{x^2 - 3x + 6}{x^2 + 5x + 1} \right)^{x/2}.$$

$$11.13. \lim_{x \rightarrow \infty} \left(\frac{3x^2 - 6x + 7}{3x^2 + 20x - 1} \right)^{-x+1}.$$

$$11.14. \lim_{x \rightarrow \infty} \left(\frac{x+3}{x+5} \right)^{x+4}.$$

$$11.15. \lim_{x \rightarrow \infty} \left(\frac{2x^2 + 21x - 7}{2x^2 + 18x + 9} \right)^{2x+1}.$$

$$11.16. \lim_{x \rightarrow \infty} \left(\frac{3x^2 + 4x - 1}{3x^2 + 2x + 7} \right)^{2x+5}.$$

$$11.17. \lim_{x \rightarrow \infty} \left(\frac{x-10}{x+1} \right)^{3x+1}.$$

$$11.18. \lim_{x \rightarrow \infty} \left(\frac{6x-7}{6x+4} \right)^{3x+2}.$$

$$11.19. \lim_{x \rightarrow \infty} \left(\frac{x^3 + 1}{x^3 - 1} \right)^{2x-x^3}.$$

$$11.20. \lim_{x \rightarrow \infty} \left(\frac{10x-3}{10x-1} \right)^{5x}.$$

$$11.21. \lim_{x \rightarrow \infty} \left(\frac{x^3 + x + 1}{x^3 + 2} \right)^{2x^2}.$$

$$11.22. \lim_{x \rightarrow \infty} \left(\frac{3x^2 - 5x}{3x^2 - 5x + 7} \right)^{x+1}.$$

$$11.23. \lim_{x \rightarrow \infty} \left(\frac{13x+3}{13x-10} \right)^{x-3}.$$

$$11.24. \lim_{x \rightarrow \infty} \left(\frac{x+3}{x+1} \right)^{-x^2}.$$

$$11.25. \lim_{x \rightarrow \infty} \left(\frac{2x^2 + 2x + 3}{2x^2 + 2x + 1} \right)^{3x^2 - 7}.$$

$$11.26. \lim_{x \rightarrow \infty} \left(\frac{x^2 - 6x + 5}{x^2 - 5x + 5} \right)^{3x + 2}.$$

$$11.27. \lim_{x \rightarrow \infty} \left(\frac{7x^2 + 18x - 15}{7x^2 + 11x + 15} \right)^{x + 2}.$$

$$11.28. \lim_{x \rightarrow \infty} \left(\frac{x + 4}{x + 2} \right)^x.$$

$$11.29. \lim_{x \rightarrow \infty} \left(\frac{2x - 1}{2x + 1} \right)^{x + 1}.$$

$$11.30. \lim_{x \rightarrow \infty} \left(\frac{x + 5}{x - 7} \right)^{x/6 + 1}.$$

Задача 12. Найти предел.

$$12.1. \lim_{x \rightarrow 0} \frac{7^{2x} - 5^{3x}}{x}.$$

$$12.2. \lim_{x \rightarrow 0} \frac{e^{3x} - e^{-2x}}{2x}.$$

$$12.3. \lim_{x \rightarrow 0} \frac{8^x - 4^{-3x}}{3x}.$$

$$12.4. \lim_{x \rightarrow 0} \frac{e^{7x} - e^{-2x}}{x}.$$

$$12.5. \lim_{x \rightarrow 0} \frac{6^{2x} - 7^{-2x}}{3x}.$$

$$12.6. \lim_{x \rightarrow 0} \frac{5x}{\ln(1 - 7x)}.$$

$$12.7. \lim_{x \rightarrow 0} \frac{3^{2x} - 5^{3x}}{x^3}.$$

$$12.8. \lim_{x \rightarrow 0} \frac{\ln(1 - 7x)}{2x}.$$

$$12.9. \lim_{x \rightarrow 0} \frac{6x}{\ln(1 - 5x)}.$$

$$12.10. \lim_{x \rightarrow 0} \frac{5^{3x} - 3^{-5x}}{5x}.$$

$$12.11. \lim_{x \rightarrow 0} \frac{e^x - e^{-3x}}{2x}.$$

$$12.12. \lim_{x \rightarrow 0} \frac{\ln(1 - 9x)}{5x}.$$

$$12.13. \lim_{x \rightarrow 0} \frac{2x}{\ln(1 - 3x)}.$$

$$12.14. \lim_{x \rightarrow 0} \frac{3x}{e^{-3x} - e^{-x}}.$$

$$12.15. \lim_{x \rightarrow 0} \frac{5^{2x} - 2^{3x}}{\ln(3x + 1)}.$$

$$12.16. \lim_{x \rightarrow 0} \frac{e^x - e^{-4x}}{2x}.$$

$$12.17. \lim_{x \rightarrow 0} \frac{-x}{3^{-2x} - 4^{-5x}}.$$

$$12.18. \lim_{x \rightarrow 0} \frac{3x}{\ln(1 - 6x)}.$$

$$12.19. \lim_{x \rightarrow 0} \frac{x}{e^{5x} - e^{-2x}}.$$

$$12.20. \lim_{x \rightarrow 0} \frac{\ln(1 - 12x)}{3x}.$$

$$12.21. \lim_{x \rightarrow 0} \frac{e^{12x} - e^{-3x}}{3x}.$$

$$12.22. \lim_{x \rightarrow 0} \frac{12^x - 5^{-3x}}{2x}.$$

$$12.23. \lim_{x \rightarrow 0} \frac{4^{5x} - 9^{-2x}}{5x}.$$

$$12.24. \lim_{x \rightarrow 0} \frac{7x}{e^{5x} - e^{-4x}}.$$

$$12.25. \lim_{x \rightarrow 0} \frac{\ln(1 - 4x)}{x}.$$

$$12.26. \lim_{x \rightarrow 0} \frac{3^{3x} - 7^{-7x}}{8x}.$$

$$12.27. \lim_{x \rightarrow 0} \frac{e^{5x} - e^{3x}}{4x}.$$

$$12.28. \lim_{x \rightarrow 0} \frac{8x}{8^{-2x} - 6^x}.$$

$$12.29. \lim_{x \rightarrow 0} \frac{2^{2x} - 5^{-5x}}{7x}.$$

$$12.30. \lim_{x \rightarrow 0} \frac{8x}{\ln(1 - 2x)}.$$

Задача 13. Найти предел.

$$13.1. \lim_{x \rightarrow 0} \frac{e^{3x} - e^{-2x}}{2 \arcsin x - \sin x}.$$

$$13.2. \lim_{x \rightarrow 0} \frac{e^x - e^{-x}}{\sin 2x - \sin x}.$$

$$13.3. \lim_{x \rightarrow 0} \frac{e^{5x} - e^{3x}}{\sin 2x - \sin x}.$$

$$13.4. \lim_{x \rightarrow 0} \frac{3^{2x} - 5^{3x}}{\arcsin x + x^3}.$$

$$13.5. \lim_{x \rightarrow 0} \frac{6^{2x} - 7^{-2x}}{\sin 3x - 2x}.$$

$$13.6. \lim_{x \rightarrow 0} \frac{10^{2x} - 7^{-x}}{2 \sin x - \arcsin x}.$$

$$13.7. \lim_{x \rightarrow 0} \frac{7^{3x} - 3^{2x}}{\sin x + x^3}.$$

$$13.9. \lim_{x \rightarrow 0} \frac{e^{7x} - e^{-2x}}{\sin x - 2x}.$$

$$13.11. \lim_{x \rightarrow 0} \frac{e^{2x} - e^x}{\sin 2x - \sin x}.$$

$$13.13. \lim_{x \rightarrow 0} \frac{e^x - e^{-2x}}{x + \sin x^2}.$$

$$13.15. \lim_{x \rightarrow 0} \frac{e^x - e^{3x}}{\sin 3x - \sin 2x}.$$

$$13.17. \lim_{x \rightarrow 0} \frac{5^{2x} - 2^{3x}}{\sin x + \sin x^2}.$$

$$13.19. \lim_{x \rightarrow 0} \frac{e^{3x} - e^{2x}}{\sin 3x - \arcsin 2x}.$$

$$13.21. \lim_{x \rightarrow 0} \frac{e^{2x} - e^x}{\sin 3x - \sin 5x}.$$

$$13.23. \lim_{x \rightarrow 0} \frac{4^x - 2^{7x}}{\operatorname{tg} 3x - x}.$$

$$13.25. \lim_{x \rightarrow 0} \frac{12^x - 5^{-3x}}{2 \arcsin x - x}.$$

$$13.27. \lim_{x \rightarrow 0} \frac{3^{5x} - 2^x}{x - \sin 9x}.$$

$$13.29. \lim_{x \rightarrow 0} \frac{4^x - 2^{7x}}{\sin 3x - x}.$$

$$13.8. \lim_{x \rightarrow 0} \frac{e^{2x} - e^x}{\sin 3x - \sin 5x}.$$

$$13.10. \lim_{x \rightarrow 0} \frac{3^{5x} - 2^{7x}}{\arcsin 2x - x}.$$

$$13.12. \lim_{x \rightarrow 0} \frac{3^{5x} - 2^{-7x}}{2x - \sin x}.$$

$$13.14. \lim_{x \rightarrow 0} \frac{9^x - 2^{3x}}{\sin 2x - 7x}.$$

$$13.16. \lim_{x \rightarrow 0} \frac{e^{2x} - e^x}{x + \sin x^2}.$$

$$13.18. \lim_{x \rightarrow 0} \frac{2^{3x} - 3^{2x}}{x + \arcsin x^3}.$$

$$13.20. \lim_{x \rightarrow 0} \frac{e^{5x} - e^x}{\arcsin x + x^3}.$$

$$13.22. \lim_{x \rightarrow 0} \frac{2^{3x} - 3^{5x}}{\sin 7x - 2x}.$$

$$13.24. \lim_{x \rightarrow 0} \frac{e^x - e^{-x}}{\arcsin 2x - \sin x}.$$

$$13.26. \lim_{x \rightarrow 0} \frac{e^{4x} - e^{-2x}}{2 \arcsin x - \sin x}.$$

$$13.28. \lim_{x \rightarrow 0} \frac{e^{2x} - e^{3x}}{\arcsin x - x^2}.$$

$$13.30. \lim_{x \rightarrow 0} \frac{7^{2x} - 5^{3x}}{2x - \sin 3x}.$$

Задача 14. Найти предел.

$$14.1. \lim_{x \rightarrow 0} \left(1 - \ln(1 + x^3)\right)^{\frac{3}{x^2 \arcsin x}}.$$

$$14.2. \lim_{x \rightarrow 0} \left(\cos \sqrt{x}\right)^{\frac{1}{x}}.$$

$$14.3. \lim_{x \rightarrow 0} \left(1 - \ln(1 + \sqrt[3]{x})\right)^{\frac{x}{\sin^4 \sqrt[3]{x}}}.$$

$$14.4. \lim_{x \rightarrow 0} (\cos \pi x)^{\frac{1}{x \sin \pi x}}.$$

$$14.5. \lim_{x \rightarrow 0} \left(1 + \sin^2 3x\right)^{\frac{1}{\ln \cos x}}.$$

$$14.6. \lim_{x \rightarrow 0} \left(\operatorname{tg}\left(\frac{\pi}{4} - x\right)\right)^{\operatorname{ctg} x}.$$

$$14.7. \lim_{x \rightarrow 0} \left(\frac{1 + x2^x}{1 + x3^x}\right)^{\frac{1}{x^2}}.$$

$$14.8. \lim_{x \rightarrow 0} \left(1 - x \sin^2 x\right)^{\frac{1}{\ln(1 + \pi x^3)}}.$$

$$14.9. \lim_{x \rightarrow 0} \left(2 - 5^{\arcsin x^3}\right)^{\frac{(\operatorname{cosec} x)}{x}}.$$

$$14.10. \lim_{x \rightarrow 0} \left(2 - \cos 3x\right)^{\frac{1}{\ln(1 + x^2)}}.$$

$$14.11. \lim_{x \rightarrow 0} \left(2 - 3^{\operatorname{arctg}^2 \sqrt{x}}\right)^{\frac{2}{\sin x}}.$$

$$14.12. \lim_{x \rightarrow 0} \left(2 - e^{\sin x}\right)^{\operatorname{ctg} \pi x}.$$

$$14.13. \lim_{x \rightarrow 0} \left(\cos x\right)^{\frac{1}{\ln(1 + \sin^2 x)}}.$$

$$14.14. \lim_{x \rightarrow 0} \left(\frac{1 + \sin x \cos \alpha x}{1 + \sin x \cos \beta x}\right)^{\operatorname{ctg}^3 x}$$

$$14.15. \lim_{x \rightarrow 0} \left(2 - e^{x^2}\right)^{1/\ln\left(1 + \operatorname{tg}^2\left(\frac{\pi x}{3}\right)\right)}.$$

$$14.16. \lim_{x \rightarrow 0} \left(3 - 2 \cos x\right)^{-\operatorname{cosec}^2 x}.$$

$$14.17. \lim_{x \rightarrow 0} \left(2 - 3^{\sin^2 x}\right)^{\frac{1}{\ln \cos x}}.$$

$$14.18. \lim_{x \rightarrow 0} \sqrt[2]{2 - \cos x}.$$

$$14.19. \lim_{x \rightarrow 0} \left(6 - \frac{5}{\cos x}\right)^{\operatorname{ctg}^2 x}.$$

$$14.20. \lim_{x \rightarrow 0} \left(3 - \frac{2}{\cos x}\right)^{\operatorname{cosec}^2 x}.$$

$$14.21. \lim_{x \rightarrow 0} \left(5 - \frac{4}{\cos x} \right)^{\frac{1}{\sin^2 3x}}.$$

$$14.22. \lim_{x \rightarrow 0} \left(1 - \ln \left(1 + \sqrt[3]{x} \right) \right)^{\frac{x}{\sin^4 \sqrt[3]{x}}}.$$

$$14.23. \lim_{x \rightarrow 0} \left(\frac{1 + \sin x \cos 2x}{1 + \sin x \cos 3x} \right)^{\frac{1}{\sin x^3}}.$$

$$14.24. \lim_{x \rightarrow 0} \left(2 - e^{x^2} \right)^{\frac{1}{1 - \cos \pi x}}.$$

$$14.25. \lim_{x \rightarrow 0} \left(1 + \ln \frac{1}{3} \operatorname{arctg}^6 \sqrt{x} \right)^{\frac{1}{x^3}}.$$

$$14.26. \lim_{x \rightarrow 0} \left(\frac{1 + \operatorname{tg} x \cos 2x}{1 + \operatorname{tg} x \cos 5x} \right)^{\frac{1}{x^3}}.$$

$$14.27. \lim_{x \rightarrow 0} \left(1 - \ln \cos x \right)^{\frac{1}{\operatorname{tg}^2 x}}.$$

$$14.28. \lim_{x \rightarrow 0} \left(1 + \operatorname{tg}^2 x \right)^{\frac{1}{\ln(1+3x^2)}}.$$

$$14.29. \lim_{x \rightarrow 0} \left(1 - \sin^2 \frac{x}{2} \right)^{\frac{1}{\ln(1+\operatorname{tg}^2 3x)}}.$$

$$14.30. \lim_{x \rightarrow 0} \left(\frac{1 + x3^x}{1 + x7^x} \right)^{\frac{1}{\operatorname{tg}^2 x}}.$$

Задача 15. Сравнить бесконечно малые.

$$15.1. \begin{aligned} f(x) &= \operatorname{tg} 2x, \\ g(x) &= \arcsin x. \end{aligned}$$

$$15.2. \begin{aligned} f(x) &= 1 - \cos x, \\ g(x) &= 3x^2. \end{aligned}$$

$$15.3. \begin{aligned} f(x) &= \operatorname{arctg}^2 3x, \\ g(x) &= 4x^2. \end{aligned}$$

$$15.4. \begin{aligned} f(x) &= \sin 3x - \sin x, \\ g(x) &= 5x. \end{aligned}$$

$$15.5. \begin{aligned} f(x) &= \cos 3x - \cos x, \\ g(x) &= 5x^2. \end{aligned}$$

$$15.6. \begin{aligned} f(x) &= x^2 - \cos 2x, \\ g(x) &= 6x^2. \end{aligned}$$

$$15.7. \begin{aligned} f(x) &= \sqrt{1+x} - 1, \\ g(x) &= 2x. \end{aligned}$$

$$15.8. \begin{aligned} f(x) &= \sin x + \sin 5x, \\ g(x) &= 2x. \end{aligned}$$

$$15.9. \quad \begin{aligned} f(x) &= 3x/(1-x), \\ g(x) &= x/(x+4). \end{aligned}$$

$$15.10. \quad \begin{aligned} f(x) &= 3x^2/(2+x), \\ g(x) &= 7x^2. \end{aligned}$$

$$15.11. \quad \begin{aligned} f(x) &= 2x^3, \\ g(x) &= 5x^3/(4-x). \end{aligned}$$

$$15.12. \quad \begin{aligned} f(x) &= x^2/(5+x), \\ g(x) &= 4x^2/(x-1). \end{aligned}$$

$$15.13. \quad \begin{aligned} f(x) &= \sin 8x, \\ g(x) &= \arcsin 5x. \end{aligned}$$

$$15.14. \quad \begin{aligned} f(x) &= \sin 3x + \sin x, \\ g(x) &= 10x. \end{aligned}$$

$$15.15. \quad \begin{aligned} f(x) &= \cos 7x - \cos x, \\ g(x) &= 2x^2. \end{aligned}$$

$$15.16. \quad \begin{aligned} f(x) &= 1 - \cos 2x, \\ g(x) &= 8x^2. \end{aligned}$$

$$15.17. \quad \begin{aligned} f(x) &= 3\sin^2 4x, \\ g(x) &= x^2 - x^4. \end{aligned}$$

$$15.18. \quad \begin{aligned} f(x) &= \operatorname{tg}(x^2 + 2x), \\ g(x) &= x^2 + 2x. \end{aligned}$$

$$15.19. \quad \begin{aligned} f(x) &= \arcsin(x^2 - x), \\ g(x) &= x^3 - x. \end{aligned}$$

$$15.20. \quad \begin{aligned} f(x) &= \sin 7x + \sin x, \\ g(x) &= x. \end{aligned}$$

$$15.21. \quad \begin{aligned} f(x) &= \sqrt{4+x} - 2, \\ g(x) &= 3x. \end{aligned}$$

$$15.22. \quad \begin{aligned} f(x) &= \sin(x^2 - 2x), \\ g(x) &= x^4 - 8x. \end{aligned}$$

$$15.23. \quad \begin{aligned} f(x) &= 2x/(3-x), \\ g(x) &= 2x - x^2. \end{aligned}$$

$$15.24. \quad \begin{aligned} f(x) &= x^2/(7+x), \\ g(x) &= 3x^3 - x^2. \end{aligned}$$

$$15.25. \quad \begin{aligned} f(x) &= \sin(x^2 + 5x), \\ g(x) &= x^3 - 25x. \end{aligned}$$

$$15.26. \quad \begin{aligned} f(x) &= \cos x - \cos^3 x, \\ g(x) &= 6x^2. \end{aligned}$$

$$15.27. \quad \begin{aligned} f(x) &= \arcsin 2x, \\ g(x) &= 8x. \end{aligned}$$

$$15.28. \quad \begin{aligned} f(x) &= 1 - \cos 4x, \\ g(x) &= x \sin 2x. \end{aligned}$$

$$15.29. \quad \begin{aligned} f(x) &= \sqrt{9-x} - 3, \\ g(x) &= 2x. \end{aligned}$$

$$15.30. \quad \begin{aligned} f(x) &= \cos 3x - \cos 5x, \\ g(x) &= x^2. \end{aligned}$$

Задача 16. Найти пределы, используя эквивалентные бесконечно малые функции.

$$16.1. \quad \lim_{x \rightarrow 0} \frac{\ln(1+3x^2)}{x^3 - 5x^2}.$$

$$16.2. \quad \lim_{x \rightarrow 0} \frac{\sin 7x - \sin 3x}{e^x}.$$

$$16.3. \quad \lim_{x \rightarrow 0} \frac{1 - \cos 3x}{\sin^2 7x}.$$

$$16.4. \quad \lim_{x \rightarrow 0} \frac{x^2}{\ln(x^2 + 1)}.$$

$$16.5. \quad \lim_{x \rightarrow 0} \frac{\arcsin 2x}{\ln(2x^2 + 1)}.$$

$$16.6. \quad \lim_{x \rightarrow 0} \frac{\ln(1 + 4x^2)}{\sin 4x}.$$

$$16.7. \quad \lim_{x \rightarrow 0} \frac{3x^2 - 5x}{\sin 3x}.$$

$$16.8. \quad \lim_{x \rightarrow 0} \frac{1 - \cos 4x}{2x^2}.$$

$$16.9. \quad \lim_{x \rightarrow 0} \frac{\ln(1+3x)}{\sqrt{8x+1} - 1}.$$

$$16.10. \quad \lim_{x \rightarrow 0} \frac{\sin 7x}{\ln(7x+1)}.$$

$$16.11. \quad \lim_{x \rightarrow 0} \frac{\sqrt{1+x} - 1}{3 \arcsin 3x}.$$

$$16.12. \quad \lim_{x \rightarrow 0} \frac{\log_3(x+1)}{\arcsin x}.$$

$$16.13. \quad \lim_{x \rightarrow 0} \frac{3^{5x} - 1}{\sin 6x}.$$

$$16.14. \quad \lim_{x \rightarrow 0} \frac{1 - \cos 5x}{\sin^2 x}.$$

$$16.15. \quad \lim_{x \rightarrow 0} \frac{1 - 9^{-2x}}{\sin 6x}.$$

$$16.16. \quad \lim_{x \rightarrow 0} \frac{\ln(1+2x)}{\sqrt{3x+1} - 1}.$$

$$16.17. \quad \lim_{x \rightarrow 0} \frac{1 - \cos 3x}{\log_3(6x^2 + 1)}.$$

$$16.18. \quad \lim_{x \rightarrow 0} \frac{1 - e^{2x}}{\sin 3x}.$$

$$16.19. \lim_{x \rightarrow 0} \frac{1 - e^{2x^2}}{1 - \cos 3x}.$$

$$16.20. \lim_{x \rightarrow 0} \frac{\sin 2x + 2 \sin x}{1 - \cos 5x}.$$

$$16.21. \lim_{x \rightarrow 0} \frac{1 - \cos 7x}{\sin^2 2x}.$$

$$16.22. \lim_{x \rightarrow 0} \frac{10^{2x} - 1}{2 \arcsin 3x}.$$

$$16.23. \lim_{x \rightarrow 0} \frac{\sqrt{1+6x} - 1}{\sin 7x}.$$

$$16.24. \lim_{x \rightarrow 0} \frac{1 - e^{7x^2}}{\sin^2 3x}.$$

$$16.25. \lim_{x \rightarrow 0} \frac{\log_3(3x+1)}{\arcsin 2x}.$$

$$16.26. \lim_{x \rightarrow 0} \frac{1 - \cos 2x}{\sin^2 x}.$$

$$16.27. \lim_{x \rightarrow 0} \frac{e^{5x} - 1}{\arcsin x}.$$

$$16.28. \lim_{x \rightarrow 0} \frac{5x^2 - x}{\arcsin 3x}.$$

$$16.29. \lim_{x \rightarrow 0} \frac{\ln(x^2 + 1)}{1 - \sqrt{2x^2 + 1}}.$$

$$16.30. \lim_{x \rightarrow 0} \frac{1 - \cos 2x}{\arcsin^2 7x}.$$

Задача 17. Найти точки разрыва функции y и определить их тип.

$$17.1. y = e^{\frac{1}{x-7}}.$$

$$17.2. y = \ln(x-8).$$

$$17.3. y = \frac{\sqrt{3x+4} - 1}{2x^2 - 5x - 7}.$$

$$17.4. y = \frac{|x-4|}{x^2 + x - 20}.$$

$$17.5. y = 5^{\frac{1}{11-x}}.$$

$$17.6. y = \operatorname{arctg}\left(\frac{1}{x+9}\right).$$

$$17.7. y = \frac{\sqrt{21+x} - 5}{x^2 - 16}$$

$$17.8. y = x + \frac{x+3}{|x+3|}$$

$$17.9. y = \arctg \frac{1}{3-x}$$

$$17.11. y = \ln(x+7)$$

$$17.13. y = \frac{2-2x}{x^3-x^4}$$

$$17.15. y = x + \frac{x+2}{|x+2|}$$

$$17.17. y = \frac{x}{|x|}$$

$$17.19. y = \arctg \frac{1}{x-2}$$

$$17.21. y = \frac{|x+1|}{x^2+x^3}$$

$$17.23. y = \frac{x-1}{2x^2-x-1}$$

$$17.25. y = \frac{1}{1+e^{\frac{1}{x-1}}}$$

$$17.27. y = x + \frac{x-5}{|x-5|}$$

$$17.29. y = 3^{\frac{1}{1-x}}$$

$$17.10. y = e^{\frac{1}{x+5}}$$

$$17.12. y = \frac{\sqrt{20+x}-5}{x^2-25}$$

$$17.14. y = e^{\frac{1}{x+1}}$$

$$17.16. y = \frac{x^2}{x-2}$$

$$17.18. y = \frac{\sqrt{7+x}-3}{x^2-4}$$

$$17.20. y = \frac{4x}{x+3}$$

$$17.22. y = \frac{|x|}{x-x^3}$$

$$17.24. y = \arctg \frac{1}{x}$$

$$17.26. y = \ln(1+2x)$$

$$17.28. y = \arctg \frac{1}{x-6}$$

$$17.30. y = \frac{3}{x^2-2x}$$

Задача 18. Для кусочно-заданной функции $y = f(x)$:

- 1) найти точки разрыва функции, если они существуют;
- 2) найти скачок функции в каждой точке разрыва;
- 3) сделать схематический чертеж.

18.1.

$$y = \begin{cases} x + 2, & x < 0, \\ -x^2 + 1, & 0 \leq x \leq 1, \\ x + 5, & x > 1. \end{cases}$$

18.2.

$$y = \begin{cases} 0, & x < -\pi/2, \\ \cos x, & -\pi/2 \leq x < \pi, \\ 2, & x \geq \pi. \end{cases}$$

18.3.

$$y = \begin{cases} x - 1, & x < -1, \\ x^2 + 3, & -1 \leq x < 1, \\ -2x, & x \geq 1. \end{cases}$$

18.4.

$$y = \begin{cases} 2 - x, & x \leq -\pi/4, \\ \operatorname{tg} x, & -\pi/4 < x \leq 0, \\ 0, & x > 0. \end{cases}$$

18.5.

$$y = \begin{cases} 4 - x, & x \leq 0, \\ (x + 3)^2, & 0 < x < 2, \\ 2x, & x \geq 2. \end{cases}$$

18.6.

$$y = \begin{cases} \cos x, & x < 0, \\ x - 1, & 0 \leq x < 2, \\ 2, & x \geq 2. \end{cases}$$

18.7.

$$y = \begin{cases} x - 3, & x < 0, \\ x^2 - 1, & 0 \leq x < 1, \\ x + 6, & x \geq 1. \end{cases}$$

18.8.

$$y = \begin{cases} x + 3, & x < -\pi, \\ \sin x, & -\pi \leq x < 0, \\ 0, & x \geq 0. \end{cases}$$

18.9.

$$y = \begin{cases} 2x + 4, & x < 1, \\ 3x^2, & 1 \leq x < 3, \\ x - 2, & x \geq 3. \end{cases}$$

18.11.

$$y = \begin{cases} -4x, & x < -1, \\ -(x-1)^2, & -1 \leq x < 1, \\ 4x, & x \geq 1. \end{cases}$$

18.13.

$$y = \begin{cases} -x + 3, & x < -2, \\ x^2 - 1, & -2 \leq x < 1, \\ 2 - 4x, & x \geq 1. \end{cases}$$

18.15.

$$y = \begin{cases} x - 4, & x < -1, \\ x^2, & -1 \leq x < 1, \\ x + 4, & x \geq 1. \end{cases}$$

18.17.

$$y = \begin{cases} x, & x < 0, \\ x^2 + 1, & 0 \leq x < 1, \\ 3 - x, & x \geq 1. \end{cases}$$

18.10.

$$y = \begin{cases} 1 + x, & x < -1, \\ x^2, & -1 \leq x < 0, \\ \sin x, & x \geq 0. \end{cases}$$

18.12.

$$y = \begin{cases} 4, & x < -\pi, \\ \cos x, & -\pi \leq x < 0, \\ 0, & x \geq 0. \end{cases}$$

18.14.

$$y = \begin{cases} -1, & x \leq -\pi/4, \\ \operatorname{tg} x, & -\pi/4 < x \leq \pi/4, \\ x^2, & x > \pi/4. \end{cases}$$

18.16.

$$y = \begin{cases} x + 1, & x < -2, \\ -x^2 + 2, & -2 \leq x < 1, \\ 2 + x, & x \geq 1. \end{cases}$$

18.18.

$$y = \begin{cases} x + 1, & x \leq 0, \\ (x + 1)^2, & 0 < x \leq 2, \\ -x + 4, & x > 2. \end{cases}$$

18.19.

$$y = \begin{cases} -x^2, & x \leq -\pi/4, \\ \operatorname{tg} x, & -\pi/4 < x \leq \pi/4, \\ 2, & x > \pi/4. \end{cases}$$

18.21.

$$y = \begin{cases} \sin x, & x < 0, \\ x^2, & 0 \leq x \leq 2, \\ 0, & x > 2. \end{cases}$$

18.23.

$$y = \begin{cases} \cos x, & x < 0, \\ 1 - x, & 0 \leq x \leq 2, \\ x^2, & x > 2. \end{cases}$$

18.25.

$$y = \begin{cases} -\sin x, & x < 0, \\ x^2, & 0 \leq x < 1, \\ 2x, & x \geq 1. \end{cases}$$

18.27.

$$y = \begin{cases} 2x, & x \leq 1, \\ (x-1)^2, & 1 < x < 3, \\ 2-2x, & x \geq 3. \end{cases}$$

18.20.

$$y = \begin{cases} x+2, & x \leq -1, \\ x^2+1, & -1 < x \leq 1, \\ -x+3, & x > 1. \end{cases}$$

18.22.

$$y = \begin{cases} -x, & x \leq 0, \\ -(x-1)^2, & 0 < x < 2, \\ x-3, & x \geq 2. \end{cases}$$

18.24.

$$y = \begin{cases} x+4, & x < -1, \\ x^2+2, & -1 \leq x < 1, \\ 2x, & x \geq 1. \end{cases}$$

18.26.

$$y = \begin{cases} x-1, & x < -1, \\ -2, & -1 \leq x < 0, \\ \cos x, & x \geq 0. \end{cases}$$

18.28.

$$y = \begin{cases} \sin x, & x < -\pi, \\ \cos x, & -\pi \leq x < \pi, \\ 1, & x \geq \pi. \end{cases}$$

18.29.

$$y = \begin{cases} -x, & x \leq -\pi/4, \\ \operatorname{tg} x, & -\pi/4 < x \leq \pi/4, \\ x, & x > \pi/4. \end{cases}$$

18.30.

$$y = \begin{cases} -x-1, & x < 0, \\ (x+5)^2, & 0 \leq x < 3, \\ 1-x, & x \geq 3. \end{cases}$$

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